



ISTITUTO ITALIANO  
DI TECNOLOGIA

**AUTOMATIC KINEMATIC CHAIN**

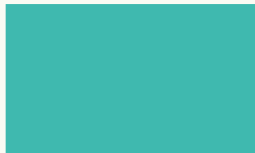
**CALIBRATION USING ARTIFICIAL SKIN:**

**SELF-TOUCH IN THE ICUB**

**HUMANOID ROBOT**

**Alessandro Roncone**

Matej Hoffmann, Ugo Pattacini, Giorgio Metta



# INDUSTRIAL ROBOT CALIBRATION .



## TARGET:

Robot kinematics in Denavit Hartenberg notation

## METHODS:

**OPEN LOOP** → external metrology system

**CLOSED LOOP** → physical constraints that act as ground truth

## CONTEXT:

(usually) well defined and very constrained

# THE ICUB IS DIFFERENT !

AND HUMANOID ROBOTS AS WELL

1 COMPLEXITY

2 RELIABILITY

3 MEASUREMENTS

# THE ICUB IS DIFFERENT !

AND HUMANOID ROBOTS AS WELL

COMPLEXITY

need for **FREQUENT** calibrations

1

RELIABILITY

need for **AUTOMATIC** methods

2

MEASUREMENTS

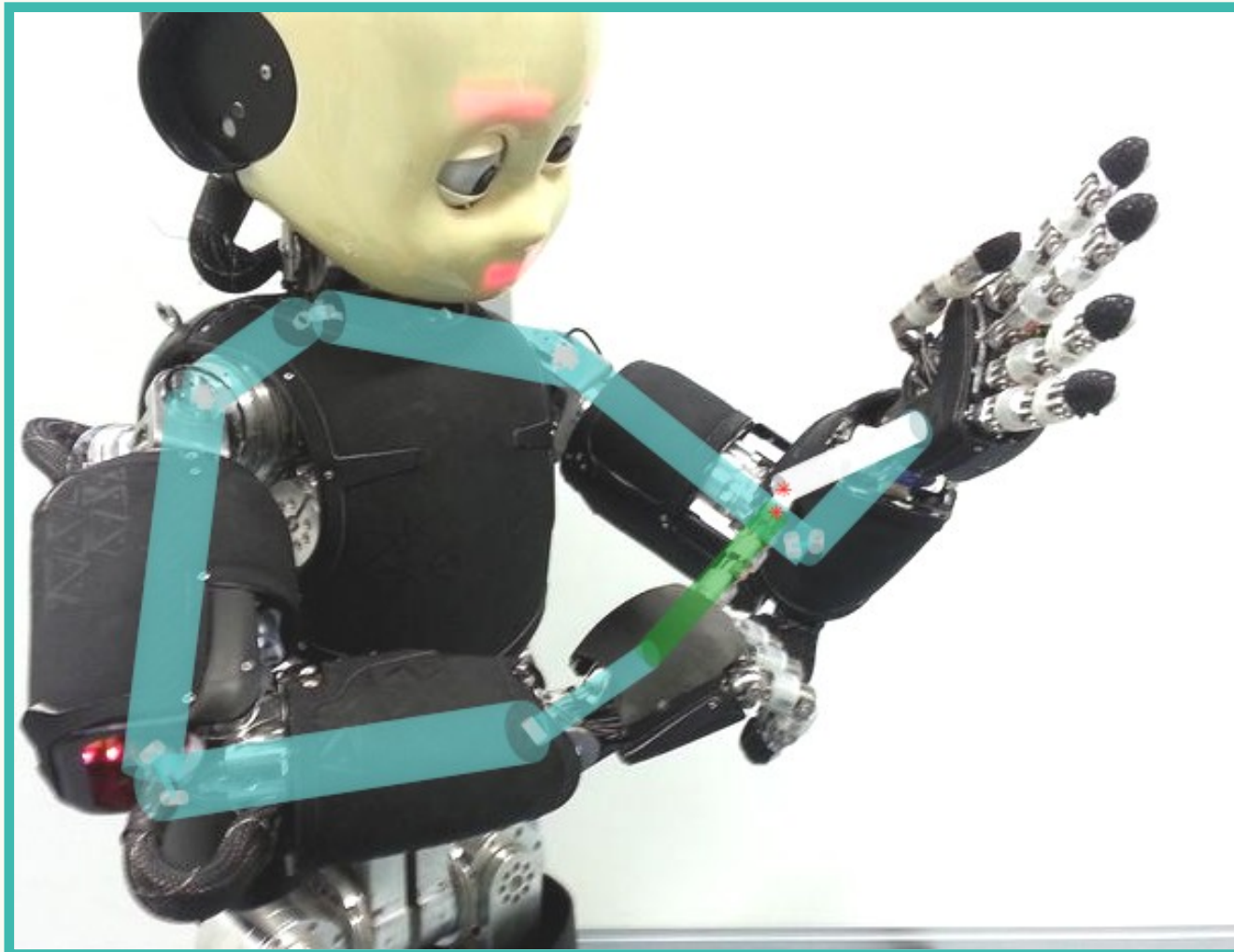
new **SENSORS** to play with

3

4

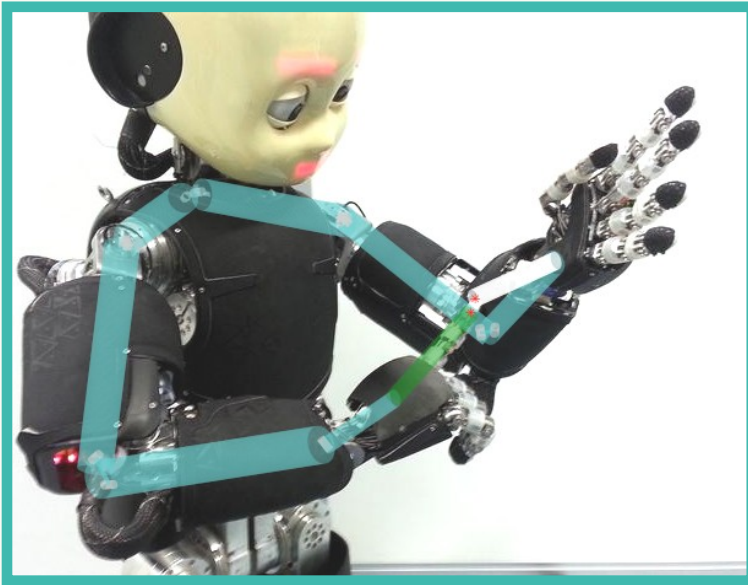
# DOUBLE TOUCH .

AS A SELF-CONTAINED CLOSED LOOP CALIBRATION METHOD



# DOUBLE TOUCH .

AS A SELF-CONTAINED CLOSED LOOP CALIBRATION METHOD



it is a **CLOSED LOOP** method

1

**SKIN** is the ground truth

2

no need for **EXTERNAL METROLOGY SYSTEMS**

3

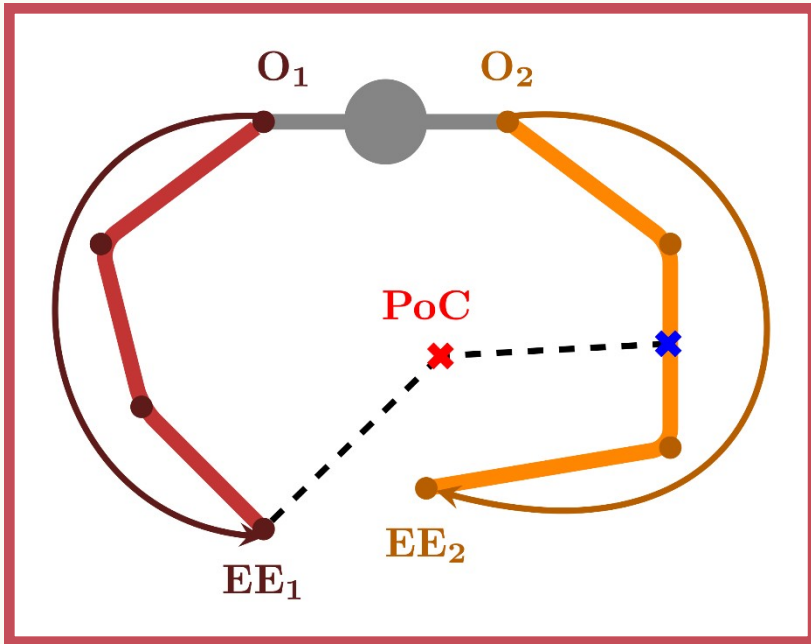
6



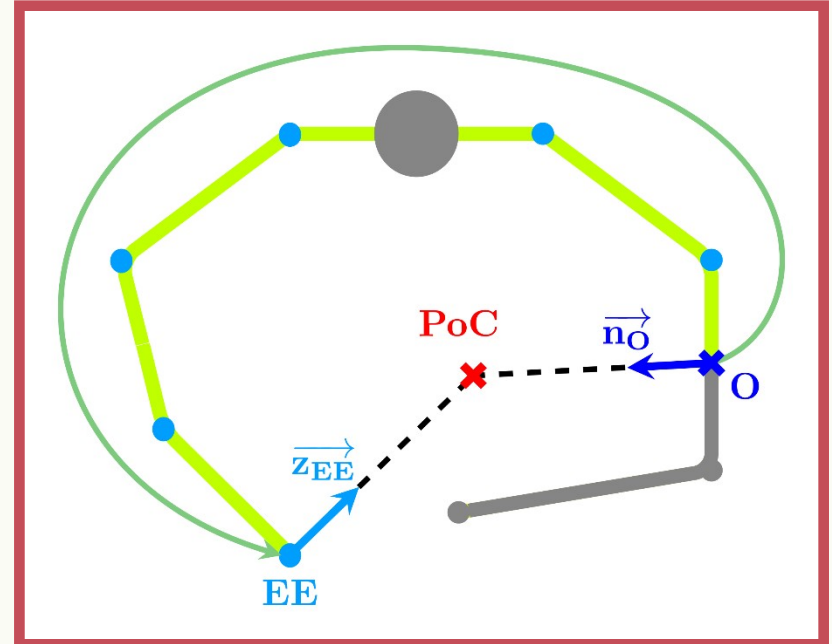
# METHOD

# KINEMATIC CHAIN REFORMULATION .

FROM TWO FIXED-BASE PARALLEL ARMS TO A  
SINGLE FLOATING-BASE SERIAL CHAIN



CLASSIC APPROACH



PROPOSED APPROACH



# KINEMATIC CHAIN REFORMULATION .

FROM TWO FIXED-BASE PARALLEL ARMS TO A  
SINGLE FLOATING-BASE SERIAL CHAIN

1

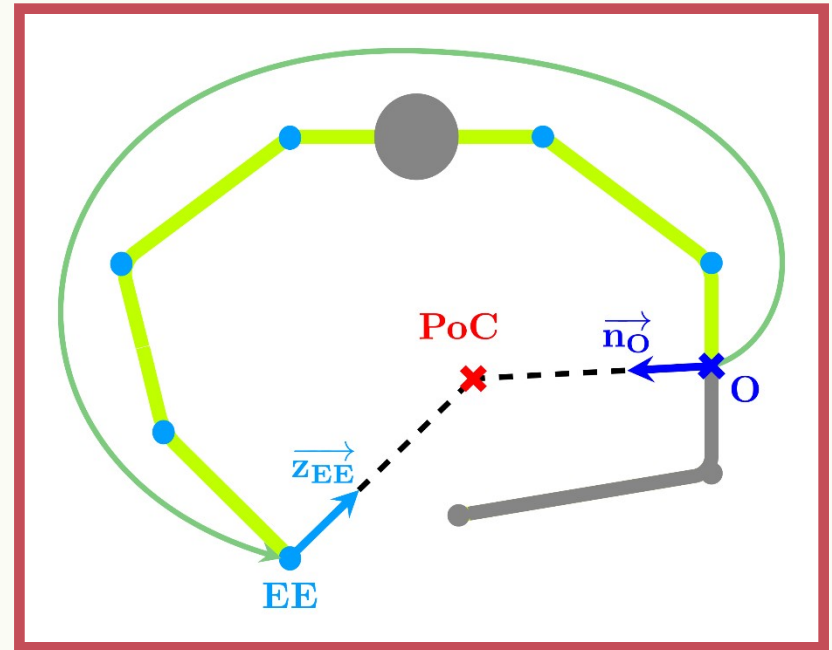
FLOATING BASE

2

MORE DOFs

3

STANDARD IK TECHNIQUES

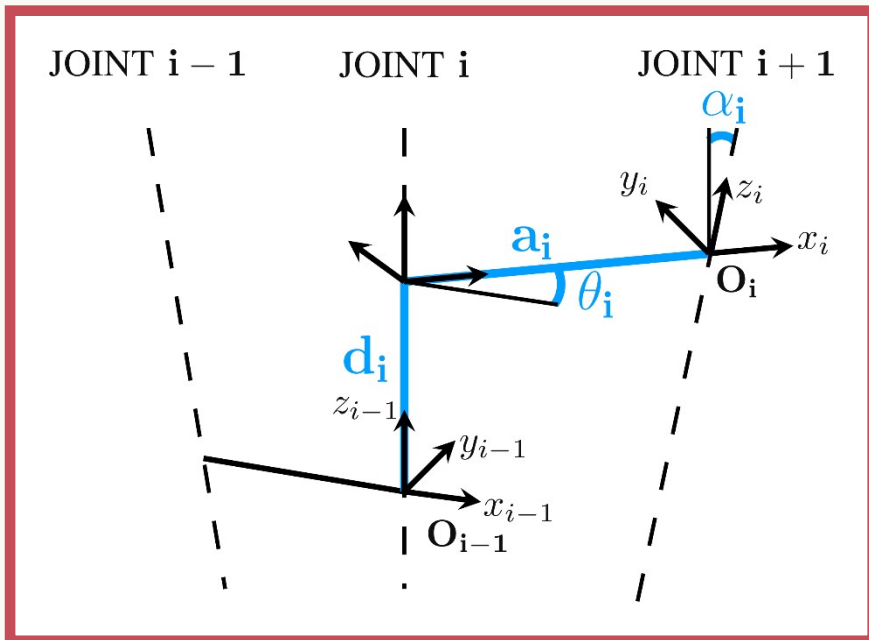


# DENAVIT-HARTENBERG "REVERSION" .

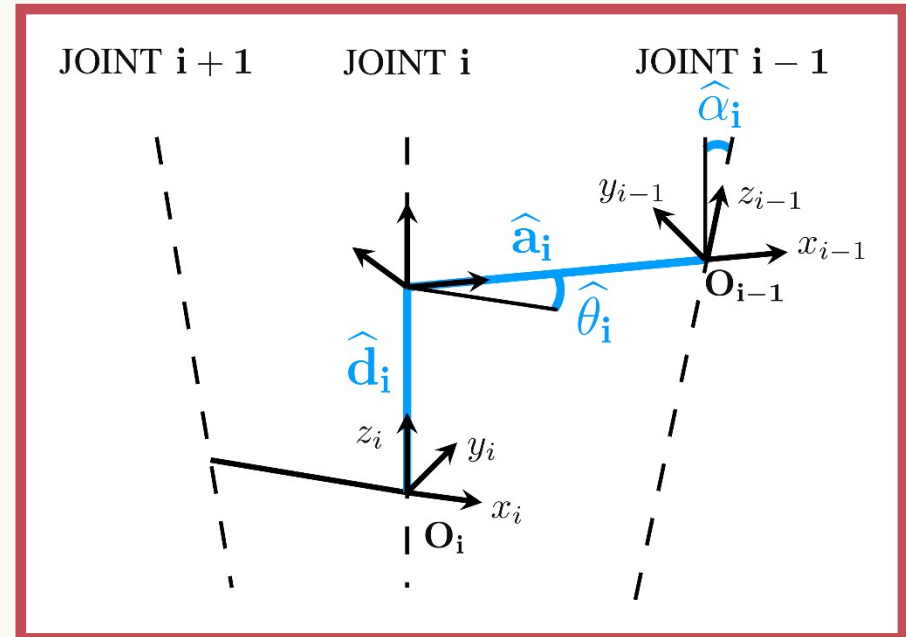
IT'S NOT AN INVERSION .

$$\Phi_i = \{a_i, d_i, \alpha_i, \theta_i\}$$

$$\hat{\Phi}_i = \{\hat{a}_i, \hat{d}_i, \hat{\alpha}_i, \hat{\theta}_i\}$$



**ORIGINAL (DIRECT) D-H**  
[from right to left]



**"REVERSED" D-H**  
[from left to right]

# DENAVIT-HARTENBERG "REVERSION" .

IT'S NOT AN INVERSION .

$$dDH = \begin{bmatrix} c_\theta & -s_\theta c_\alpha & s_\theta s_\alpha & a c_\theta \\ s_\theta & c_\theta c_\alpha & -c_\theta s_\alpha & a s_\theta \\ 0 & s_\alpha & c_\alpha & d \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$rDH = \begin{bmatrix} c_{\hat{\theta}} & -s_{\hat{\theta}} & 0 & \hat{a} \\ s_{\hat{\theta}} c_{\hat{\alpha}} & c_{\hat{\theta}} c_{\hat{\alpha}} & -s_{\hat{\alpha}} & -\hat{d} s_{\hat{\alpha}} \\ s_{\hat{\theta}} s_{\hat{\alpha}} & c_{\hat{\theta}} s_{\hat{\alpha}} & c_{\hat{\alpha}} & \hat{d} c_{\hat{\alpha}} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

ORIGINAL (DIRECT) D-H

"REVERSED" D-H

$$\begin{aligned} \langle \hat{\mathbf{a}}_0, \hat{\mathbf{a}}_1, \dots, \hat{\mathbf{a}}_n \rangle &= \langle -\mathbf{a}_n, -\mathbf{a}_{n-1}, \dots, -\mathbf{a}_0 \rangle \\ \langle \hat{\mathbf{d}}_0, \hat{\mathbf{d}}_1, \dots, \hat{\mathbf{d}}_n \rangle &= \langle -\mathbf{d}_n, -\mathbf{d}_{n-1}, \dots, -\mathbf{d}_0 \rangle \\ \langle \hat{\alpha}_0, \hat{\alpha}_1, \dots, \hat{\alpha}_n \rangle &= \langle -\alpha_n, -\alpha_{n-1}, \dots, -\alpha_0 \rangle \\ \langle \hat{\theta}_0, \hat{\theta}_1, \dots, \hat{\theta}_n \rangle &= \langle -\theta_n, -\theta_{n-1}, \dots, -\theta_0 \rangle \end{aligned}$$

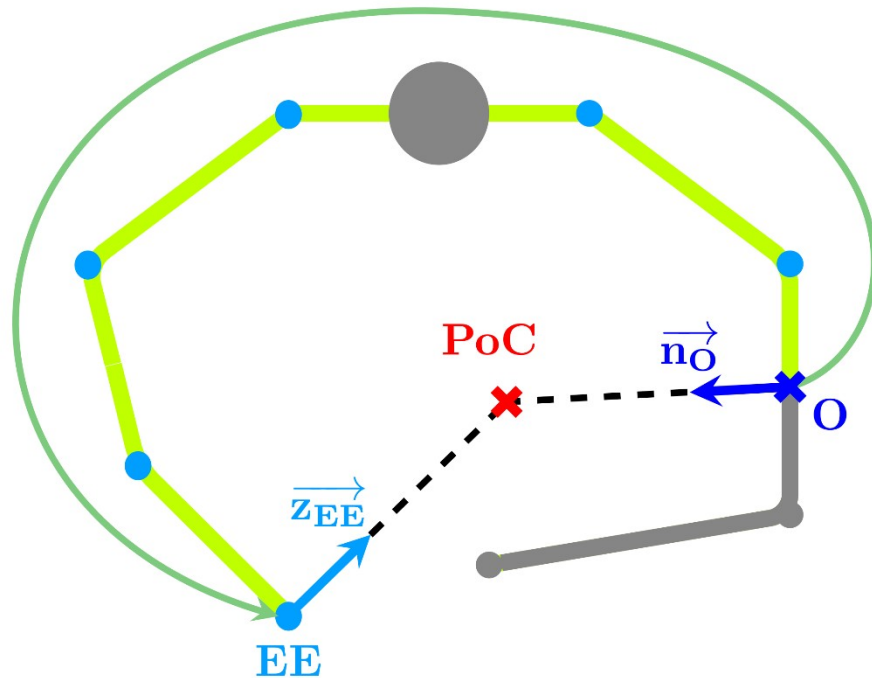
# INVERSE KINEMATIC SOLVER .

5+7 = 12 DoFs

$$\mathbf{q}^* = \arg \min_{\mathbf{q} \in \mathbb{R}^n} \langle \mathbf{n}_O, \mathbf{z}_{EE} \rangle =$$

$$= \arg \min_{\mathbf{q} \in \mathbb{R}^n} \left\{ \|\mathbf{n}_O\| \cdot \|\mathbf{z}_{EE}\| \cdot \cos(\alpha) \right\}$$

$$s.t. \begin{cases} \|K_x(\mathbf{q}) - \mathbf{O}\|^2 < \epsilon \\ \mathbf{q}_l < \mathbf{q} < \mathbf{q}_u \end{cases}$$



IPOPT

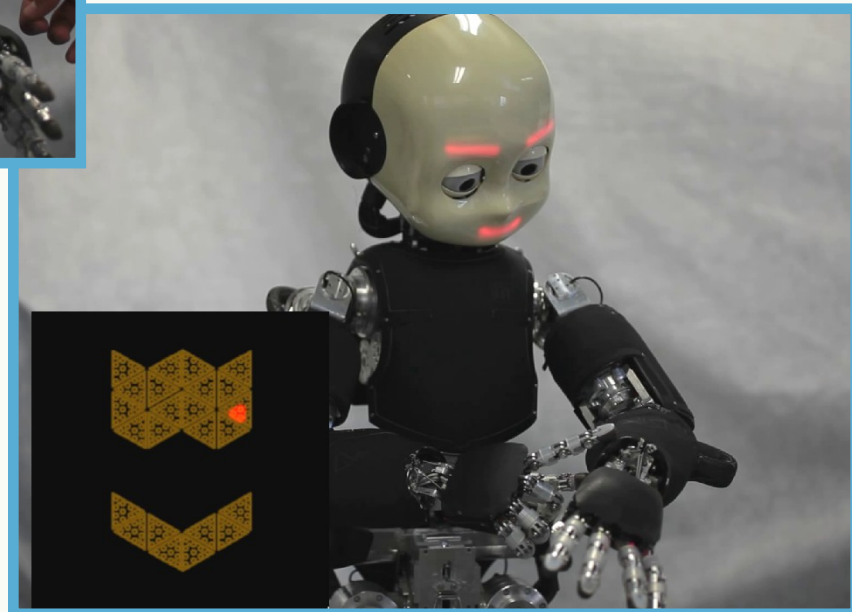
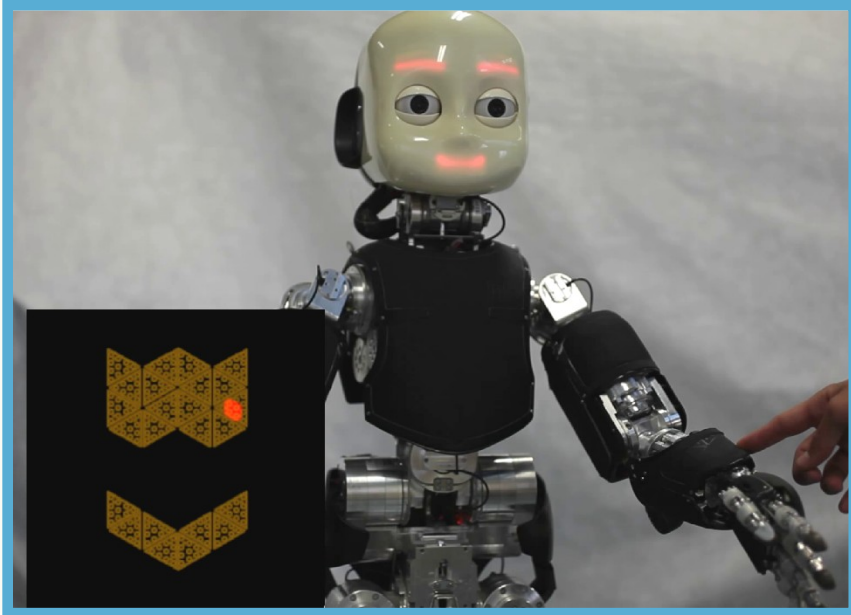
# CALIBRATION .

$$\bar{\Phi}^* = \mathit{arg} \min_{\Phi} \sum_{m=1}^M \|\mathbf{p}_s - \mathbf{p}_e(\Phi, \theta_m)\|$$



# RESULTS

# EXPERIMENTS .



# EXPERIMENTS .

$$\Phi^* = \arg \min_{\Phi} \sum_{m=1}^M \|\mathbf{p}_s - \mathbf{p}_e(\Phi, \theta_m)\|$$

**M=300** samples

DH from CAD model

10% noise

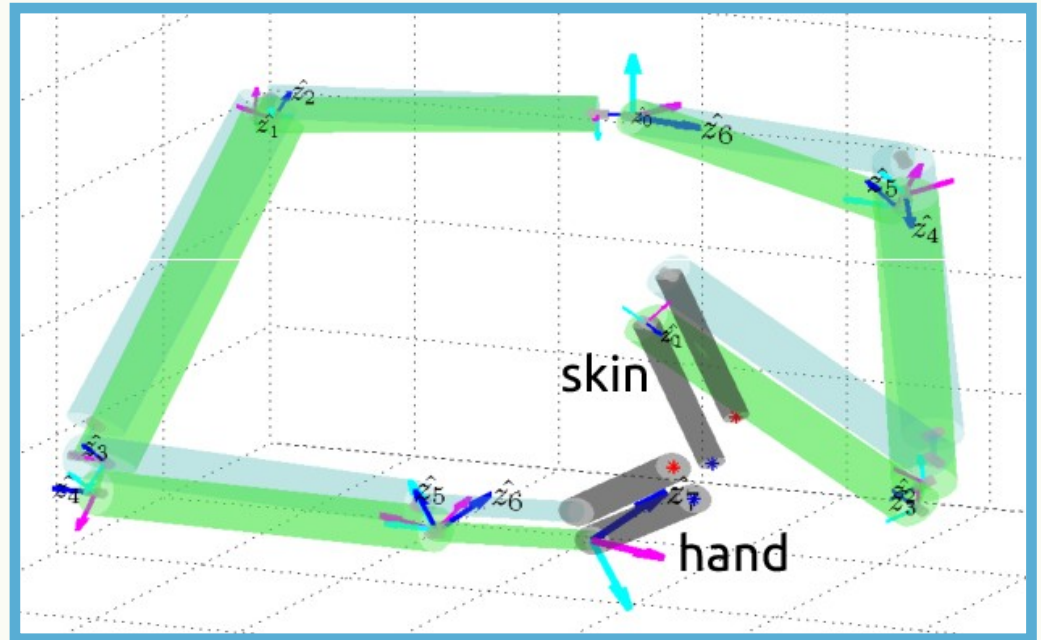
30 % noise

3 EXP.

**12x4=48** parameters



# RESULTS .



	INITIAL ERROR [m]	OPTIMIZED ERROR [m]
EXP 1 (DH model)	0.0226	0.0208
EXP 2 (10% noise)	$0.0819 \pm 0.0299$	$0.0377 \pm 0.0139$
EXP 3 (30% noise)	$0.1919 \pm 0.0301$	$0.0664 \pm 0.0175$